Advanced Microeconomics - Problem set 1
Due date: classes on October 16, 2018
Problem 1 Compute supply and profit as functions of the price vector $\left(p_{a}, p_{b}\right)$ for the following production set:

$$
Y=\left\{(a, b, c) \in \mathbb{R}^{3} \mid a \leq 0, b \leq 0, c \leq \min \{-\alpha a,-\beta b\}^{\gamma}\right\}, \text { where } \alpha, \beta, \gamma>0 .
$$

Problem 2 In a three-commodity economy, we consider a producer whose cost function is

$$
C\left(p_{a}, p_{b}, c\right)=2 c^{2} p_{a}^{\frac{2}{3}} p_{b}^{\frac{1}{3}}
$$

Compute supply and profit of this producer as functions of the price vector $\left(p_{a}, p_{b}, p_{c}\right)$.
Problem 3 In a two -commodity economy, we consider a producer with the following production set:

$$
Y_{\alpha}=\left\{(a, b) \in \mathbb{R}^{2} \mid a \leq 0, b \leq \sqrt{-a+\alpha}-\sqrt{\alpha}\right\}, \text { where } \alpha \geq 0 .
$$

a) Determine profit and supply of this producer as functions of the price vector $\left(p_{a}, p_{b}\right)$.
b) Assume that there is a second producer whose production set is $Y_{\beta}$ with $\beta \geq \alpha$. What is the aggregate supply of this economy as a function of the price vector $\left(p_{a}, p_{b}\right)$ ?

Problem 4 In a three-good economy, a firm has two production units. The first one produces commodity $C$ using commodity $A$ as an input. The production set of this unit is:

$$
\left\{(a, b, c) \in \mathbb{R}^{3}|a \leq 0, b \leq 0, c \leq|a|\} .\right.
$$

The second unit produces commodity $C$ using commodity $B$ as an input. The production set of this unit is:

$$
\left\{(a, b, c) \in \mathbb{R}^{3} \mid a \leq 0, b \leq 0, c \leq b^{2}\right\}
$$

a) Determine the iso-output set, i.e. the set of input baskets for which the output is at least $c$, where $c \geq 0$ is some given value.
b) Compute the cost function and the demand of inputs as functions of the vector ( $c, p_{a}, p_{b}$ ).
c) Compute the supply of this firm as a function of the price vector $\left(p_{a}, p_{b}, p_{c}\right)$.

